#### High School (9-12)



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# **Curriculum Map: Mathematics**

**Course:** Honors Geometry

Grade(s): 9

# **Unit 1:** Tools of Geometry

# **Brief Summary of Unit**

# **Stage One—Desired Results**

**Established Goals:** (Standards of Learning, Content Standards)

- 1. Complete patterns using inductive reasoning and make conjectures
- 2. Name basic geometric figures and identify types of angles
- 3. Find the length of segments using the ruler and segment addition postulates
- 4. Find the measure of unknown angles using the angle addition postulate
- 5. Find the distance or midpoint between 2 points using the distance or midpoint formula
- 6. Find perimeter and area of squares, rectangles, and circles using the formulas

#### **Understandings:**

- 1. Lengths of segments can be found using the ruler postulate or the distance formula depending on where the segment is (space or coordinate plane).
- 2. Other formulas and properties can help in finding the perimeter and area of various figures.
- 3. Geometry is a mathematical system built on accepted facts, basic terms, and definitions.
- 4. Special angle pairs can be used to identify geometric relationships and to find angle measures.
- 5. Formulas can be used to find the midpoint and length of any segment in the coordinate plane.

#### **Essential Ouestions:**

- 1. What is the process of using inductive reasoning?
- **2.** What are the basic terms of geometry?
- **3.** What are the relationships between the basic building blocks of geometry?
- **4.** What are segments and rays and parallel lines?
- **5.** What is the distance between two points in a coordinate plane?
- **6.** What is the midpoint of two points in a coordinate plane?
- 7. What is the perimeter of a geometric figure?
- **8.** What is the area of a geometric figure?

6. Perimeter and area are two different ways of measuring the size of geometric figures.

Stage Two—Assessment Evidence

Performance Tasks:

Other Evidence: :(quizzes, tests and so on)

Stage Three—Learning Plan

**Unit 2:** Reasoning and Proof

# **Brief Summary of Unit**

# **Stage One—Desired Results**

**Established Goals:** (Standards of Learning, Content Standards)

- 1. Justify steps in a logical argument
- 2. Use the Law of Detachment
- 3. Use the Law of Syllogism
- 4. Write biconditionals
- 5. Recognize 'good' definitions
- 6. Recognize conditional statements
- 7. Write converse/inverse/negations of conditional statements
- 8. Connect reasoning in algebra and geometry
- 9. Write two-column proofs involving algebraic properties

# **Understandings:**

- 1. How deductive reasoning works and how to use it to form algebraic conclusions
- 2. Critical reading is based on logic.
- 3. Patterns in some number sequences and some sequences of geometric figures can be used to discover relationships.
- 4. Some mathematical relationships can be described using a variety of if-then statements.
- 5. Algebraic properties of equality are used in geometry to solve problems and justify reasoning.
- 6. Given information, definitions, properties, postulates, and previously proven theorems can be used as reasons in a proof.

# **Essential Questions:**

- 1. How can you make a conjecture and prove that it is true?
- **2.** What is the difference(s) between deductive and inductive reasoning?
- **3.** How does deductive reasoning lead to logical conclusions?

# Stage Two—Assessment Evidence

#### **Performance Tasks:**

Other Evidence: :(quizzes, tests and so on)

Stage Three—Learning Plan

# **Unit 3:** Parallel & Perpendicular Lines

# **Brief Summary of Unit**

# **Stage One—Desired Results**

Established Goals: (Standards of Learning, Content Standards)

- 1. Graph linear equations / functions
- 2. Write linear equations using various given information
- 3. Make predictions from linear models
- 4. Write linear equation of parallel and perpendicular lines.
- 5. Identify the different special pairs of angles formed by two lines and a transversal.
- 6. (alternate interior, alternate exterior, same-side interior, corresponding, vertical, linear pairs)

# **Understandings:**

# 1. Linear equations represent and model real world situations.

- 2. Comparing the slopes of two lines can show whether the lines are parallel or perpendicular.
- 3. A line can be graphed and its equation written when certain facts about the line, such as its slope and a point on a line are known.
- 4. Predictions can be made about real world situations using linear relationships.
- 5. Not all lines and not all planes intersect.
- 6. When a line intersects two or more lines, the angles formed at intersection points create special angle pairs.
- 7. Certain angle pairs can be used to decide whether two lines are parallel.
- 8. The relationships of two lines to a third line can be used to decide whether two lines are parallel or perpendicular to each other.

# **Essential Questions:**

- 1. How do you prove that two lines are parallel or perpendicular?
- **2.** How do you write an equation of a line in the coordinate plane?

# **Stage Two—Assessment Evidence**

#### **Performance Tasks:**

**Other Evidence:** :(quizzes, tests and so on)

# Stage Three—Learning Plan

# **Unit 4:** Congruent Triangles

# **Brief Summary of Unit**

# **Stage One—Desired Results**

Established Goals: (Standards of Learning, Content Standards)

- 1. Identify congruent polygons and name the corresponding parts
- 2. Identify congruent triangles using the congruence postulates (SSS, SAS, ASA, AAS), HL Theorem
- 3. Use CPCTC to identify that corresponding parts of congruent triangles are congruent
- 4. Identify an isosceles triangle using the theorem and its converse
- 5. Find unknown parts of triangles using the isosceles triangle theorem and its converse

# **Understandings:**

- 1. Various properties and theorems can be used in addition to the congruence postulates and theorems in order to identify congruent polygons.
- 2. Comparing the corresponding parts of two figures can show whether the figures are congruent.
- 3. Two triangles can be proven to be congruent without having to show that all corresponding parts are congruent.
- 4. Unknown parts of triangles can be found using CPCTC, properties, and theorems of triangles.
- 5. The angles and sides of isosceles and equilateral triangles have special relationships.

# **Essential Questions:**

- 1. How do you identify corresponding parts of congruent triangles?
- **2.** How do you show that two triangles are congruent?
- **3.** How can you tell whether a triangle is isosceles or equilateral?

#### Stage Two—Assessment Evidence

**Performance Tasks:** 

**Other Evidence:** :(quizzes, tests and so on)

# **Stage Three—Learning Plan**

# **Unit 5:** <u>Triangle Relationships</u>

# **Brief Summary of Unit**

# **Stage One—Desired Results**

# **Established Goals:** (Standards of Learning, Content Standards)

- 1. Use properties of midsegments to solve problems
- 2. Use properties of perpendicular bisectors and angle bisectors
- 3. Identify properties of perpendicular bisectors, angle bisectors, medians, and altitudes
- 4. Use inequalities involving angles of triangles
- 5. Use inequalities involving sides of triangles

# **Understandings:**

- 1. Perpendicular bisectors, angle bisectors, medians, and altitudes have similarities and differences.
- 2. The measures of the angles of a triangle are related to the lengths of the opposite sides.
- 3. Properties and theorems of midsegments, perpendicular bisectors, angle bisectors, medians, and altitudes can be used to find unknown lengths and angle measures in triangles.
- 4. In triangles that have two pairs of congruent sides, there is a relationship between the included angles and the third pair of sides.

# **Essential Questions:**

- **1.** How do you use coordinate geometry to find relationships within triangles?
- **2.** How do you solve problems that involve measurements of triangles?
- **3.** How do you write indirect proofs?

# Stage Two—Assessment Evidence

**Performance Tasks:** 

**Other Evidence:** :(quizzes, tests and so on)

# **Stage Three—Learning Plan**

# Unit 6: Quadrilaterals

# **Brief Summary of Unit**

# **Stage One—Desired Results**

**Established Goals:** (Standards of Learning, Content Standards)

- 1. Define and classify special types of quadrilaterals
- 2. Use relationships among sides and among angles of parallelograms
- 3. Use relationships involving diagonals of parallelograms or transversals
- 4. Determine whether a quadrilateral is a parallelogram and specify a type of parallelogram
- 5. Use properties of diagonals of rhombuses and rectangles and properties of trapezoids and kites.

# **Understandings:**

# **Essential Questions:**

1. Given information can be used to classify quadrilaterals.

1. How can you find the sum of the measures of polygon angles?

- 2. Parallelograms have special properties regarding their sides, angles, and diagonals.
- 3. If a quadrilateral's sides, angles, and diagonals have certain properties, it can be shown that the quadrilateral is a parallelogram.
- 4. Variables can be used to name the coordinates of a figure in the coordinate plane. This allows relationships to be shown to be true for a general case.

- **2.** How can you classify quadrilaterals?
- **3.** How can you use coordinate geometry to prove general relationships?

# **Stage Two—Assessment Evidence**

Performance Tasks:

**Other Evidence:** :(quizzes, tests and so on)

# Stage Three—Learning Plan

# Unit 7: Area

# **Brief Summary of Unit**

# **Stage One—Desired Results**

**Established Goals:** (Standards of Learning, Content Standards)

- 1. Calculate the area of various polygons
- 2. Calculate the area of a circle
- 3. Find missing dimensions of diagrams using formulas
- 4. Calculate geometric probability given a figure
- 5. Calculate lengths of arcs in circles
- 6. Calculate areas of sectors in circles

# **Understandings:**

- 1. Missing parts of right triangles can be found using the Pythagorean Theorem or properties of special right triangles.
- 2. In some cases, dimensions required to calculate area must be derived using other formulas.
- 3. Geometric probability is used to make decisions about complex problems.
- 4. Ratios can be used to compare the perimeters and areas of similar figures.
- 5. The area formula for a rectangle can be used to derive the area formulas for triangles, parallelograms, trapezoids, kites, and circles.

#### **Essential Questions:**

- 1. How do you find the area of polygon?
- **2.** How do you find the circumference of a circle?
- **3.** How do you find the area of a circle?
- **4.** How do perimeters and areas of similar polygons compare?

# Stage Two—Assessment Evidence Performance Tasks: Other Evidence: :(quizzes, tests and so on) Stage Three—Learning Plan

**Unit 8:** Similarity

# **Brief Summary of Unit**

# Stage One—Desired Results

**Established Goals:** (Standards of Learning, Content Standards)

- 1. Write ratios of similar figures
- 2. Set up and solve proportions of similar figures using the properties of proportions
- 3. Find unknown lengths using indirect measurement
- 4. Solve proportions using theorems of similar triangles
- 5. Find the ratio of similarity, perimeters, and area using the others
- 6. Use the AA, SAS, SSS similarity postulates to show triangles are similar.

# **Understandings:**

- 1. Ratios and proportions can be used to solve complex problems in such things as scale drawings and indirect measurement.
- 2. The Golden Ratio appears in everyday life in many common occurrences.
- 3. The ratio of similarity in similar figures can be used to find unknown lengths, the perimeter ratio (perimeter), and area ratio (area).
- 4. Ratios and proportions can be used to decide whether two polygons are similar and to find unknown side lengths of similar figures.
- 5. Drawing in the altitude to the hypotenuse of a right triangle forms three pairs of similar right triangles.
- 6. When two or more parallel lines intersect other lines, proportional segments are formed.

# **Essential Questions:**

- 1. How do you show two triangles are similar?
- **2.** How do you identify corresponding parts of similar triangles?

# Stage Two—Assessment Evidence

#### Performance Tasks:

**Other Evidence:** :(quizzes, tests and so on)

# **Stage Three—Learning Plan**

# **Unit 9: Surface Area & Volume**

# **Brief Summary of Unit**

# **Stage One—Desired Results**

Established Goals: (Standards of Learning, Content Standards)

- 1. Identify the parts on a polyhedron
- 2. Find unknown number of faces, edges, or vertices using Euler's Formula
- 3. Find the surface area and volume of prisms, cylinders, pyramids, cones, and spheres
- 4. Find the volume of composite figures
- 5. Find the slant height or height in pyramids and cones using the Pythagorean Theorem

# **Understandings:**

- 1. Surface area and volume of threedimensional objects can be used to solve complex problems.
- 2. A three-dimensional figure can be analyzed by describing the relationships among its vertices, edges, and faces.
- 3. The surface area of a three-dimensional figure is equal to the sum of the areas of each surface of the figure.
- 4. The volume of a pyramid is related to the volume of a prism with the same base and height.
- 5. Ratios can be used to compare the areas and volumes of similar solids.

# **Essential Questions:**

- **1.** How can you determine the intersection of solid and a plane?
- **2.** How do you find the surface area and volume of a solid?
- **3.** How do the surface areas and volumes of similar solids compare?

# Stage Two—Assessment Evidence

**Performance Tasks:** 

**Other Evidence:** :(quizzes, tests and so on)

#### Stage Three—Learning Plan

# **Unit 10: CIRCLES**

#### **Brief Summary of Unit**

#### **Stage One—Desired Results**

**Established Goals:** (Standards of Learning, Content Standards)

- 1. Find lengths and angle measures using the Tangent Theorem and its converse
- 2. Find the missing lengths of a triangle that is circumscribed about the circle
- 3. Find the distance from the center of the circle to the chord or the length of a chord using the theorems
- 4. Find missing angle and arc measures using the inscribed angle theorem
- 5. Find missing segment lengths using the theorem about segments in circles

# **Understandings:**

- 1. Missing angle measures, arc measures, and segment lengths can be found using the various theorems.
- 2. A radius of a circle and the tangent that intersects the endpoint of the radius on the circle have a special relationship.
- 3. Information about congruent parts of a circle (or congruent circles) can be used to find information about other parts of the circle (or circles).
- 4. The information of the equation of a circle allows the circle to be graphed. The equation of a circle can be written if its center and radius are known..

## **Essential Questions:**

- 1. How can you prove relationships between angles and arcs in a circle?
- **2.** When lines intersect a circle, or within a circle, how do you find the measures of resulting angles, arcs, and segments?
- **3.** How do you find the equation of a circle in the coordinate plane?

# Stage Two—Assessment Evidence

## **Performance Tasks:**

**Other Evidence:** :(quizzes, tests and so on)

# Stage Three—Learning Plan

# **Unit 11: Right Triangle Trigonometry**

# **Brief Summary of Unit**

# **Stage One—Desired Results**

Established Goals: (Standards of Learning, Content Standards)

- 1. Write sine, cosine, tangent ratios in reference to the parts of a right triangle.
- 2. Calculate missing side lengths and angles of a right triangle, given minimal information, by using the trigonometric ratios.
- 3. Use angles of elevation and depression to solve problems.
- 4. Describe vectors in terms of magnitude and direction.
- 5. Solve problems that involve vector addition.
- 6. Find the area of polygons using trigonometry.

# **Understandings:**

1. If the lengths of any two sides of a right triangle are known, then the third side can

#### **Essential Questions:**

**1.** How do you write sin/cos/tan ratios in terms of the sides of a right triangle?

be found by using the Pythagorean Theorem.

- 2. Certain right triangles have properties that allow the lengths of their sides to be found without using the Pythagorean Theorem.
- 3. If certain combinations of side lengths and angles of a right triangle are known, ratios can be used to find the other sides and angles
- 4. The angles of elevation and depression are the acute angles of a right triangle formed by a horizontal distance and a vertical height.
- 5. Vectors can be used to model motion and direction.
- 6. The area of regular polygons can be found using the trigonometric functions.
- 7. Indirect measurement can be used to find distances by using trigonometric ratios.
- 1. Missing angle measures, arc measures, and segment lengths can be found using the various theorems.
- 2. A radius of a circle and the tangent that intersects the endpoint of the radius on the circle have a special relationship.
- 3. Information about congruent parts of a circle (or congruent circles) can be used to find information about other parts of the circle (or circles).
- 4. The information of the equation of a circle allows the circle to be graphed.

  The equation of a circle can be written if its center and radius are known..

- **2.** How is trigonometry used to find missing distances in real-world situations?
- **3.** How is vector addition used to solve problems?

	Stage	Two—A	Assessment	Evid	lenc
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Other Evidence: :(quizzes, tests and so on)

# Stage Three—Learning Plan